# CHAPTER

## Ratio and Proportion, Indices and Logarithm

[1] (b) Let numbers be 2x and 3x. Therefore,  $(3x)^2$   $(2x)^2 = 320$  $9x^2$   $4x^2 = 320$  $5x^2 = 320$  $x^2 = 64$ x = 8Numbers are:  $2x = 2 \times 8 = 16$  $3x = 3 \times 8 = 24$ [2] (d) As per the given information :  $\frac{\mathbf{p} - \mathbf{x}^2}{\mathbf{q} - \mathbf{x}^2} = \frac{\mathbf{P}^2}{\mathbf{q}^2}$   $q^2 (\mathbf{p} \quad \mathbf{x}^2) = \mathbf{P}^2(\mathbf{q} \quad \mathbf{x}^2)$   $pq^2 \quad \mathbf{x}^2 q^2 = p^2 q \quad p^2 \mathbf{x}^2$   $\mathbf{x}^2 (\mathbf{p}^2 \quad q^2) = pq(\mathbf{p} \quad q)$  $x^{2} = \frac{\mathbf{pq} (\mathbf{p} \square \mathbf{q})}{\mathbf{p}^{2} \square \mathbf{q}^{2}}$  $x^2 = \mathbf{p} \mathbf{q}$ p+q [3] (a) Let the quantity of copper and zinc in an alloy be 9x kg and 4x kg. Therefore, 9x = 24 $x = \frac{24}{9} = \frac{8}{3} = 2\frac{2}{3} kg.$ So zine =  $4x = 4 \times \frac{8}{3} kg$ .  $= 10 \frac{2}{3} kg.$ [4] (c)  $7 \log\left(\frac{16}{15}\right) + 5 \log\left(\frac{25}{24}\right) + 3 \log\left(\frac{81}{80}\right)$ 7(log 16 log 15) + 5(log 25 log 24) +3 log (log 81 log 80) = =  $7 [4 \log 2 (\log 3 + \log 5)] + 5 [2 \log 5 (3 \log 2 + \log 3)]$  $+ 3 [4 \log 3 (4 \log 2 + \log 5)]$ = 28 log 2 7 log 3 7 log 5 + 10 log 5 15 log 2 5 log 3  $+ 12 \log 3$  12 log 2 3 log 5 = log 2

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[5] (c) Let the numbers be 7x and 8x. So,  $\frac{7x + 3}{8x + 3} = \frac{8}{9}$ 9(7x+3) = 8(8x+3)63x + 27 = 64x + 24x = 3Numbers are : 7x =7×3 =21  $8x = 8 \times 3 = 24$ [6] (a) Let the number of one rupee coins be x. Then, number of 50. paise coins is 4xand number of 25 paise coins is 2xSo.  $x + \frac{4x}{2} + \frac{2x}{4} = 56$  $4x + 8x + 2x = 56 \times 4$ 14x = 224 $x = \frac{224}{14} = 16$ Number of 50 paise coins is  $4 \times 16 = 64$ [7] (b)  $(a^{1/8} + a^{-1/8}) (a^{1/8} - a^{-1/8}) (a^{1/4} + a^{-1/4}) (a^{1/2} + a^{-1/2})$ =  $(a^{1/4} - a^{-1/4}) (a^{1/4} + a^{-1/4}) (a^{1/2} + a^{-1/2})$  $\begin{bmatrix} \text{using } (a^2 \quad b^2) = (a \ b) \ (a + b) \end{bmatrix} = (a^{1/2} \quad a^{-1/2}) \ (a^{1/2} + a^{-1/2}) = a^1 \quad a^{-1}$ = a <u>1</u> [8] (a)  $a^{\log_a^b \cdot \log_b^c \cdot \log_d^d \cdot \log_d^t}$ a  $\frac{\log^{b}}{\log^{a}} \times \frac{\log^{c}}{\log^{b}}, \frac{\log^{d}}{\log^{c}} \cdot \frac{\log^{t}}{\log^{d}} =$  using log a <sup>b</sup> =  $\frac{\log^{b}}{\log^{a}}$  $= a \frac{\log^t}{\log^a}$ =  $a \log_{a}^{t}$ = t [using  $\mathbf{a}^{\log \sigma^m} = m$ ]

[9] (b) 
$$\log_{1000} x = \frac{1}{4}$$
  
 $(10,000)^{-1/4}$   $x = [using log a^b = x, = a^x = b$   
 $\frac{1}{(10,000)^{1/4}} = x$   
 $= \frac{1}{10} = x$   
[10] (c) When number of people = 8  
then, the share of each person  $= \frac{1}{8}$  of the total cost.  
When number of people = 7  
then, the share of each person  $= \frac{1}{7} \square \frac{1}{8} = \frac{1}{56}$  i.e.  
 $\frac{1}{7}$  of  $\frac{1}{8}$ , i.e.  $\frac{1}{7}$  of the original share of each person.  
[11] (a) Let the number of coins be  $3x,4x,and 5x$ .  
Then,  $3x + \frac{4x}{2} + \frac{5x}{10} = 187$   
 $30x + 20x + 5x = 187 \times 10$   
 $55x = 1870$   
 $x = \frac{1870}{55} = 34$   
Number of coins:  
One rupee  $= 3x = 3 \times 34 = 102$   
 $50 \text{ paise } = 4x = 4 \times 34 = 136$   
 $10 \text{ paise } = 5x = 5 \times 34 = 170$   
[12] (b)  $\frac{x^{m \cdot 3n} \cdot x^{4m - 9n}}{x^{6m - 6n}} \left[ \text{ using } \frac{x \cdot \Pi x}{x^{a \cdot b}} \right]$   
 $= \frac{x^{5m - 6n}}{x^{6m - 6n}} \left[ \text{ using } \frac{x \cdot \Pi x}{x^{a \cdot b}} \right]$ 

$$= x^{5m-6n-6m+6n} \left[ using \frac{x^{a}}{x^{b}} = x^{a-b} \right]$$

$$= x^{m}$$
[13] (a) Log (2a 3b) = log a log b  
log (2a 3b) = log  $\left(\frac{a}{b}\right)$ 
2a 3b =  $\frac{a}{b}$   
2ab 3b<sup>2</sup> = a  
2ab 3b<sup>2</sup> = a  
2ab a = 3b<sup>2</sup>  
a(2b 1) = 3b<sup>2</sup>  
a =  $\frac{3b^{2}}{2b\Box 1}$ 
[14] (c)  $\frac{1}{1+z^{a-b}+z^{a-c}} + \frac{1}{1+z^{b-c}+z^{b-a}} + \frac{1}{1+z^{c-a}+z^{c-b}}$   

$$= \frac{1}{1+\frac{z^{-b}}{z^{-a}} + \frac{z^{-c}}{z^{-a}}} + \frac{1}{1+\frac{z^{-c}}{z^{-b}}} + \frac{z^{-a}}{z^{-b}} + \frac{1}{1+\frac{z^{-a}}{z^{-b}}} + \frac{z^{-b}}{z^{-c}}$$

$$= \frac{z^{-a}+z^{-b}+z^{-c}}{z^{-a}+z^{-b}+z^{-c}} + \frac{z^{-b}}{z^{-b}+z^{-c}+z^{-a}} + \frac{z^{-c}}{z^{-c}+z^{-a}+z^{-b}+z^{-c}}$$

$$= \frac{1}{1}$$
[15] (d) Let the earning of A and B be 4x and 7x respectively.  
New earning of A = 4x × 150% = 6x  
New earning of A = 7x × 75% = 5.25  
Then,  $\frac{6x}{5.25x} = \frac{8}{7}$   
This does not give the value of x  
So, the given data is inadequate.  
[16] (b)  $\frac{P}{Q} = \frac{11}{12}$  and  $\frac{P}{R} = \frac{9}{8}$   
 $\frac{P}{Q} = \frac{11\times9}{12\times9} = \frac{99}{108}$  and  $\frac{P}{R} = \frac{9\times11}{8\times11} = \frac{99}{88}$ 

Therefore, 
$$\frac{Q}{R} = \frac{108}{88} = \frac{27}{22}$$
  
So, Q:R = 27:22  
[17] (c)  $\frac{1}{\log(abc)} + \frac{1}{\log(abc)} + \frac{1}{\log(abc)}$   
 $= \frac{\frac{1}{\log(abc)} + \frac{1}{\log(abc)} + \frac{1}{\log(abc)}}{\log(bc)} + \frac{1}{\log(abc)}$   
 $\left[ using \log_a b = \frac{\log b}{\log a} \right]$   
 $= \frac{\log(ab)}{\log(abc)} + \frac{\log(bc)}{\log(abc)} + \frac{\log(ca)}{\log(abc)}$   
 $= \frac{\log(ab \times bc \times ca)}{\log(abc)}$   
 $= \frac{\log(ab \times bc \times ca)}{\log(abc)}$   
 $= \frac{\log(abc)^2}{\log(abc)} = \frac{2\log(abc)}{\log(abc)} = 2$   
[18] (c)  $2^{64}$   
 $= 64 \log 2$   
 $= 64 \times 0.30103$   
 $= 19.26592$   
Number of digit in  $2^{64} = 20$ .  
[19] (a) The ratio of share of A, B and C  
 $= \frac{1}{4} \cdot \frac{1}{5} \cdot \frac{1}{6}$   
 $= \frac{15:12:10}{60} = 15:12:10$   
Therefore, A's share  $= 407 \times \frac{15}{37} = \overline{1}165$   
B's share  $= 407 \times \frac{12}{37} = \overline{1}122$   
C's share  $= 407 \times \frac{10}{37} = \overline{1}10$ 

$$= 3^{\frac{-15}{4}} \times 3^{\frac{7}{4}} \times 3^{2}$$

$$= 3^{\frac{-15}{4}} \times 7^{\frac{7}{4}} \times 3^{2}$$

$$= 3^{-2+2} = 3^{0} = 1$$
[23] (a) 
$$\frac{\log 3^{8}}{\log 3^{6}} \log_{10}^{6} \log_{10}^{4}$$

$$= \log 3^{8} \cdot \log_{10}^{6} \log_{10}^{6}$$

$$= 3\log_{3}^{2} \frac{2}{4} \log_{3}^{2} 2 \log_{10}^{2}$$

$$= \frac{3\log_{2}}{\log_{10}} \cdot \frac{1\log_{3}}{2\log_{2}} \cdot \frac{2\log_{2}}{\log_{10}}$$

$$= 3\log_{10}^{2}$$
[24] (d) Quantity of glycerine =  $40 \times \frac{3}{4} = 30$  litres  
Quantity of water =  $40 \times \frac{1}{4} = 10$  litres  
Let x litres of water be added to the mixture.  
Then, total quantity of mixture =  $(40 + x)$  litres  
total quantity of water in the mixture =  $(10 + x)$  litres.  
So,  $\frac{30}{10 + x} = \frac{2}{1}$   
 $30 = 20 + 2x$   
 $2x = 10$   
 $x = 5$  litres  
Therefore, 5 litres of water must be added to the mixture.  
[25] (d) Let the third proportional be x.

$$\frac{\mathbf{a}^2 \Box \mathbf{b}^2}{(\mathbf{a} + \mathbf{b})^2} = \frac{(\mathbf{a} + \mathbf{b})^2}{\mathbf{x}}$$

By cross multiplication  

$$x = (a+b)^{2} \frac{(a+b)^{2}}{(a^{2}\Box b^{2})}$$

$$x = \frac{(a+b)^{3}}{(a\Box b)}$$
[26] (c)  $2^{x} - 2^{x-1} = 4$   
 $2^{x} - \frac{2^{x}}{2} = 4$   
 $2^{x} \left[1 - \frac{1}{2}\right] = 4$   
 $2^{x} \left[\frac{1}{2}\right] = 4$   
 $2^{x} = 8$   
 $2^{x} = 2^{3}$   
 $\therefore x = 3$   
 $x^{x} = 3^{3}$   
 $= 27$   
[27] (a)  $x = \frac{e^{n}\Box e^{-n}}{e^{n} + e^{-n}}$   
 $\frac{1}{x} = \frac{e^{n} + e^{-n}}{e^{n}\Box e^{-n}}$   
Applying Componendo & Dividendo  
 $\frac{1+x}{1\Box x} = \frac{e^{n} + e^{-n} + e^{n}\Box e^{-n}}{e^{n} + e^{-n}\Box e^{n} + e^{-n}}$   
 $\frac{1+x}{1\Box x} = \frac{2+e^{n}}{2e^{-n}}$   
 $\frac{1+x}{1\Box x} = e^{2n} \frac{1+x}{1\Box x} = 2n$   
 $Log \left(\frac{1+x}{1\Box x}\right) = 2n, n = \frac{1}{2} Log e\left(\frac{1+x}{1\Box x}\right)$   
[28] (b) Log 144  
 $= Log (16 \times 9) = log 16 + log9$   
 $= log 2^{4} + log 3^{2}$   
 $= 4log2 + 2log3.$ 

[29] (b) Let x quantity of tea worth ₹10per kg. be mixed with y quantity worth 14 per kg.  
Total price of the mixture =10x +14y.  
and  
Total quantity of the mixture =x + y  
Average price of mixture will be 
$$\frac{10x+14y}{x+y} = 11$$
  
 $10x + 14y = 11x + 11y$   
 $3y = x$   
 $\frac{x}{y} = \frac{3}{1}$   
or x : y = 3 : 1 which is the required ratio.  
[30] (a) Let the present ages of persons be 5x & 7x .  
Eighteen years ago, their ages = 5x 18 and 7x 18.  
According to given:  
 $\frac{5x \square 18}{7x \square 18} = \frac{8}{13}$   
 $65x 234 = 56x 144$   
 $9x = 90$   
 $x = 10$   
Their present ages are  $5x = 5 \times 10 = 50$  years  
 $7x = 7 \times 10 = 70$  years.  
[31] (b)  $Z = x^{c}$   
 $Z = (y^{a})^{c}$  ( $z^{b} = y$ )  
 $Z = z^{abc}$   
 $abc = 1$  ( $x^{m} = x^{n}$  then m = n)  
[32] (c)  $Log_{2}[log_{3}(log_{2} x)] = 1$   
 $= log_{3}(log_{2} x) = 2^{1}$  (Converting into exponential form)  
 $= log_{2} x = 3^{2}$  (Converting into exponential form)  
 $= log_{2} x = 3^{2}$   
[33] (b)  $Log\left(\frac{a+b}{4}\right) = \frac{1}{2}(Log a + Log b)$   
 $Log\left(\frac{a+b}{4}\right) = log(ab)\frac{2}{2}$ 

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[Since,  $\log_a mn = \log_a m + \log_a n$  and  $n \log_a m = \log_a m^n$ ] Take antilog on both sides.  $\frac{a+b}{4} = \sqrt{ab}$ a + b = 4 √**ab** Squaring both sides  $(a + b)^2 = (4\sqrt{ab})^2$  $a^2 + b^2 + 2 ab = 16 ab$  $a^2 + b^2 = 14 ab$  $\frac{\mathbf{a}}{\mathbf{b}} + \frac{\mathbf{b}}{\mathbf{a}} = 14$ , which is the required answer [34] (a) Given : Capital invested by : A : ₹ 126,000, B : ₹ 84,000, C: ₹ 2,10,000 The ratio of their investments is : 126 : 84 : 210 = 3 : 2 : 5 Profit (at year end) = ₹ 2,42,000 gives A's Share =  $\frac{3}{10}$  × 2,42,000 = ₹ 72,600 B's Share =  $\frac{2}{10}$  × 2,42,000 = ₹ 48,400 C's Share =  $\frac{5}{10}$  × 2,42,000 = ₹ 1,21,000 [35] (c)  $\frac{p}{q} = -\frac{2}{3}$ So, P =  $\frac{-2q}{3}$ .....(i) Now,  $\frac{2p+q}{2p-q}$ Substituting the value of p from (i)  $2\left(\frac{-2q}{3}\right)+q$  $2\left(\frac{-2q}{3}\right)-q$ 

$$\frac{-4q}{3} + q$$

$$\frac{-4q}{3} - q$$

$$\frac{-4q + 3q}{3}$$

$$\frac{-4q - 3q}{3}$$

$$\frac{-4q - 3q}{3}$$

$$\frac{-q}{3} \times \frac{3}{-7q}$$

$$\frac{1}{7}$$
[36] (c) Let the fourth proportional to x, 2x, (x + 1) be t, then,  

$$\frac{x}{2x} = \frac{x+1}{t}$$

$$\frac{1}{2} = \frac{x+1}{t}$$

$$t = 2x + 2$$

$$\therefore$$
 Fourth proportional to x, 2x, (x + 1) is (2x + 2)
i.e. x: 2x:: (x + 1) : (2x + 2)  
i.e. x: 2x:: (x + 1) : (2x + 2)  
[37] (d) x = 3^{1/3} + 3^{-1/3}
......(1)  
On cubing both sides, we get  

$$x^{3} = (3^{1/3} + 3^{-1/3})^{3}$$

$$x^{3} = 3 + 3^{-1} + 3 \times 3^{1/3} \times \frac{1}{3^{1/3}} (3^{1/3} + 3^{-1/3})$$

$$x^{3} = 3 + \frac{1}{3} + 3(3^{1/3} + 3^{-1/3})$$

$$x^{3} = 3 + \frac{1}{3} + 3x [Using (1)]$$

$$x^{3} - 3x = \frac{9 + 1}{3}$$

$$3(x^{3} - 3x) = 10$$

 $\therefore 3x^3 - 9x = 10$ 

$$16x + 16 = x^{2} + x$$

$$x^{2} - 15x - 16 = 0$$

$$x^{2} - 16x + x - 16 = 0$$

$$x (x - 16) + 1 (x - 16) = 0$$

$$(x + 1) (x - 16) = 0$$

$$x = 1 \text{ or } x = 16$$
Since  $x = -1$  is not possible therefore  $x = 16$ 
[41] (b)
$$\frac{2^{n} + 2^{n-1}}{2^{n+1} - 2^{n}}$$

$$= 2^{n} (1 + \frac{1}{2})$$

$$2n (2 - 1)$$

$$= \frac{3}{2} = \frac{3}{2}$$
[42] (a)
$$2^{x} \times 3^{y} \times 5^{z} = 360. \dots (1)$$
The factors of 360 are:
$$2^{3} \times 3^{2} \times 5.$$

$$2^{3} + 3^{2} \times 5.$$

$$2^{3} \times 3^{2} \times 5.$$

$$2^{3} + 3^$$

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[46] (c) Let the number added be x  $\frac{49 + x}{2} = \frac{3}{2}$ 68 + x 4 196 + 4x = 204 + 3xx = 8 [47] (c) Let the ratio be 5x : 7x If 10 student left, Ratio became 4 : 6 5x - 10 \_ 4 7x - 10 6 30x - 60 = 28x - 402x = 20x = 10÷ No. of students in each class is 5x and 7x i.e. 50, 70 **[48] (b)**  $2 \log x + 2 \log x^2 + 2 \log x^3 + \dots$  $2[\log x + \log x^2 + \log x^3 + \dots]$  $2[\log x + 2\log x + 3\log x + .....]$ 2log x[1 + 2 + 3 ..... n]  $2 \log x \times \frac{n(n+1)}{2}$  $= n(n + 1) \log x$ **[49] (d)** 2.7777 2 + 0.7 + 0.07 + 0.007 + .....  $2 + \left(\frac{7}{10} + \frac{7}{100} + \frac{7}{1000} + \dots\right)$  $2 + 7 \left( \frac{1}{10} + \frac{1}{100} + \frac{1}{1000} + \dots \right)$ 2 + 7  $\left( \frac{1/10}{1 \square 1/10} \right)$  $= 2 + 7 \times \frac{1}{9}$  $= 2 + \frac{7}{9}$  $= \frac{18+7}{9}$  $=\frac{25}{9}$ 

$$[50] (a) \left(\frac{\log_{10} x \square 3}{2}\right) + \left(\frac{11 \square \log_{10} x}{3}\right) = 2$$

$$3 \log_{10} x 9 + 22 2 \log_{10} x = 12$$

$$\log_{10} x + 13 = 12$$

$$\log_{10} x = 1$$

$$x = 10^{-1}$$

$$[51] (a) \begin{array}{l} A = \frac{2}{5} = \frac{2k}{5k}$$

$$\frac{10A + 3B}{5A + 2B} = \frac{20k + 15k}{10k + 10k} = \frac{35k}{20k}$$

$$= \frac{35}{20}$$

$$= \frac{7}{4}$$

$$[52] (a) \quad \text{Given : n = M ! for M 2}$$

$$\frac{1}{\log_{n}^{2}} + \frac{1}{\log_{n}^{3}} + \frac{1}{\log_{n}^{4}} + \dots + \frac{1}{\log_{n}^{n}}$$
or, 
$$= \log_{n}^{2} + \log_{n}^{3} + \log_{n}^{4} + \dots + \log_{n}^{m}$$

$$(\therefore \log_{b}^{a} = \frac{1}{\log_{b}^{b}})$$

$$= \log_{n} (2 \times 3 \times 4 \times \dots \times m)$$

$$(\therefore \log^{(m)}) = \log^{m} + \log^{n})$$

$$= \log_{n} (m!)$$

$$= \log_{n}^{n}$$

$$= 1$$

$$[53] (a) \quad \text{Given : A : B = B : C}$$

$$B^{2} = A \times C$$
or 
$$B = \sqrt{A \times C}$$

$$\& A = 1,60,000; C = 2,50,000$$

$$B = \sqrt{1,60,000; C = 2,50,000}$$

$$B = 2,00,000$$

$$[54] (c) \quad \text{Sub duplicate ratio of a : 9 = \sqrt{a} : \sqrt{9}, \text{ Compound Ratio (C.R.)} = 8:15$$

$$\text{ Compound Ratio of 4:5 and sub duplicate ratio of a: 9 is given by}$$

$$C.R = \frac{4}{5} \times \frac{\sqrt{a}}{\sqrt{9}}$$

$$\frac{8}{15} = \frac{4}{5} \times \frac{\sqrt{a}}{\sqrt{9}}$$

$$\sqrt{a} = \frac{8 \times 5 \times \sqrt{9}}{15 \times 4}$$

$$\sqrt{a} = \frac{8 \times 5 \times 3}{15 \times 4}$$

$$\sqrt{a} = 2$$
On squaring  $(\sqrt{a})^2 = 2^2$ 

$$a = 4$$
[55] (a) If  $\log_2 x + \log_4 x = 6$ 

$$\frac{\log x}{\log 2} + \frac{\log x}{\log 4} = 6$$

$$\frac{\log x}{\log 2} + \frac{\log x}{2\log 2} = 6$$

$$\frac{\log x}{\log 2} + \frac{\log x}{2\log 2} = 6$$

$$\frac{\log x}{\log 2} = 6 \times \frac{2}{3}$$

$$\frac{\log x}{\log 2} = 4$$

$$\log x = 16$$
[56] (d) Given x varies inversely as square of y
i. e. x \alpha \frac{1}{y^2}
$$x = k \frac{1}{y^2}$$

$$x = \frac{k}{y^2}$$
.....(1)
Given x = 1, y = 2 then

$$1 = \frac{k}{(2)^2} \quad k = 1 \times 4 = 4$$
Now putting  $y = 6$ ,  $k = 4$  in equation (1)  
 $x = \frac{4}{6^2}$   
 $x = \frac{4}{36} = \frac{1}{9}$ 
[57] (b)  $\frac{3^{n+1} + 3^n}{3^{n+3} - 3^{n+1}} = \frac{3^n \cdot 3^1 + 3^n}{3^n \cdot 3^3 - 3^n \cdot 3^1}$   
 $= \frac{3^n (3^1 + 1)}{3^n (3^3 - 3)}$   
 $= \frac{(3 + 1)}{(27 - 3)}$   
 $= \frac{4}{24}$   
 $= \frac{1}{6}$ 
[58] (c) Given  $\log_x y = 100$  ......(1)  
 $\log_2 x = 10$ ......(2)  
Multiply eq (1) & (2)  
 $\log_y y \cdot \log_2 x = 100 \times 10$   
 $\frac{\log y}{\log x} \times \frac{\log x}{\log 2} = 1,000$   
 $\log y = 1,000 \log 2$   
 $\log y = \log 2^{1,000}$   
 $y = 2^{1,000}$   
[59] (a) If say a, b, c, d are in proportion they bear a common ratio that is  $\frac{a}{b} = \frac{c}{d}$   
Option (A)  $\frac{6}{8} = \frac{5}{7}$   
Option (B)  $\frac{7}{3} = \frac{14}{6}$ 

Option (C)  $\frac{18}{27} = \frac{12}{18}$ 

Option (D) 
$$\frac{8}{6} = \frac{12}{9}$$
  
[60] (b) If  $x^{1} (x)^{1/3} = (x^{1/3})^{x}$   
 $x^{1+1/3} = x^{\frac{1}{3}x}$   
 $x^{4/3} = x^{\frac{1}{3}x}$   
on comparing  
 $\frac{4}{3} = x^{\frac{1}{3}}$   
 $3x = 12$   $X = 4$   
[61] (d) Given  
 $\frac{1}{ab} + \frac{1}{bc} + \frac{1}{ca} =$   
 $\frac{1}{abc}$   
 $\frac{c + a + b}{abc} =$   
 $\frac{1}{abc}$   
 $a + b + c =$   
1  
taking log on both side  
log  $(a + b + c) = \log 1$   
log  $(a + b + c) = 0$   
[62] (a) Let two Nos. be x and y  
Mean proportion between x and y is 18  
So, x, 18, y, are in proportion  
 $x : 18 :: 18 : y$   
 $\frac{x}{18} = \frac{18}{y}$   
 $xy = 324$   
 $x = \frac{324}{y}$  (1)

If third proportion between x & y be 144 So, x, y, 144 are in proportion x:y::y:144  $\frac{x}{y} = \frac{y}{144}$  $y^2$  = 144x \_\_\_\_\_ (2) Putting the value of x in equation (2)  $y^2 = 144 \times \frac{324}{y}$  $y^3 = 144 \times 324$  $y = \sqrt[3]{144 \times 324}$ y =  $\sqrt[3]{6 \times 6 \times 6 \times 6 \times 6 \times 6}$  $y = 6 \times 6$ y = 36Putting y = 36 in equation (1)  $x = \frac{324}{36} = 9$ x = 9, y = 36 [63] (a) Given  $(\log_{\sqrt{x^2}})^2 = \log_x 2$  $\left(\frac{\log 2}{\log \sqrt{x}}\right)^2 = \left(\frac{\log 2}{\log x}\right)$  $\left(\frac{\log 2}{\log x^{1/2}}\right)^2 = \frac{\log 2}{\log x}$  $\left(\frac{\log 2}{\frac{1}{2}\log x}\right) = \frac{\log 2}{\log x}$  $\left(\frac{2\log 2}{\log x}\right)^2 = \left(\frac{\log 2}{\log x}\right)$ 

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	$4 \left(\frac{\log 2}{\log x}\right)^2 = \left(\frac{\log 2}{\log x}\right)^1$ $4 \frac{\log 2}{\log x} = 1$ $4 \log 2 = \log x$ $\log 2^4 = \log x$ $2^4 = x  x = 16$				
[64] (d)	Mean Proportion = $\sqrt{24 \times 54}$				
	$=\sqrt{1296}$				
[65] (0)	$= 36$ The triplicate Datio of $4 \cdot 5 = 4^3 \cdot 5^3$				
[69] (C)	The triplicate Ratio of 4 : $5 = 4^3 : 5^3$ = 64 : 125				
[66] (a)	If $\sqrt[3]{a} + \sqrt[3]{b} + \sqrt[3]{c} = 0$				
	$a^{1/3} + b^{1/3} + c^{1/3} = 0$				
	$a^{1/3} + b^{1/3} = c^{1/3}$ (i)				
	Cube on both side				
	$(a^{1/3} + b^{1/3})^3 = (c^{1/3})^3$ $(a^{1/3})^3 + (b^{1/3})^3 + 3 \cdot a^{1/3} \cdot b^{1/3} (a^{1/3} + b^{1/3}) = c$				
	$(a + b + 3a^{1/3}.b^{1/3}.(c^{1/3}) = c$				
	$a + b c 3a^{1/3} b^{1/3} c^{1/3} = c$				
	$a + b + c = 3a^{1/3}$ . $b^{1/3}$ . $c^{1/3}$				
	$\left(\frac{\mathbf{a} + \mathbf{b} + \mathbf{c}}{3}\right) = \frac{3a^{1/3} \cdot b^{1/3} \cdot c^{1/3}}{3}$				
	$\left(\frac{a+b+c}{3}\right)^3 = (a^{1/3}. b^{1/3}. c^{1/3})^3 = abc$				
[67] (a)	Since Batio of three Number is 1 : 2 : 3				
	First No. = x				
	Second No. = 2x Third No. = 3x				
	Sum of squares of numbers = 504				
	$(x)^2 + (2x)^2 + (3x)^2 = 504$				
	$x^{2} + 4x^{2} + 9x^{2} = 504$ $14x^{2} = 504$				
	14% - 504				

$$x^{2} = \frac{504}{14}$$

$$x^{2} = 36$$

$$x = 6$$
First No. = x = 6  
Second No. = 2x = 2 × 6 = 12  
Third No. = 3x = 3 × 6 = 18  
[68] (d)  $\log_{4} 9 \cdot \log_{2} 2$ 

$$= \frac{\log 9}{\log 9} \cdot \frac{\log 2}{\log 3}$$

$$= \frac{2\log 3}{2\log 2} \cdot \frac{\log 2}{\log 3}$$

$$= 1$$
[69] (c)  $(\log_{x} x \cdot \log_{2} y \cdot \log_{2} z)^{3}$ 

$$= (\frac{\log x}{\log y} \cdot \frac{\log y}{\log z})^{3}$$

$$= (1)^{3}$$

$$= 1$$
[70] (c) The sum of two No. = 80  
First No. = x  
Second No. = (80 x)  
Product two No = x. (80 x)  
Product

$$2x = 80$$
  
 $x = 40$   
 $x = 40$  in equation (iii)  

$$\frac{d^{2}p}{dx^{2}} = 2$$
 (Negative)  
function is maximum at  $x = 40$   
Numbers are 40, (80 40)  
 $= 40, 40$   
[71] (b) Given,  
 $x : y = 2 : 3$   
Let  $x = 2k, y = 3k$   
 $(5x + 2y) : (3x y)$   
 $= \frac{5 \times 2k + 2 \times 3k}{3 \times 2k - 3k}$   
 $= \frac{10k + 6k}{6k - 3k}$   
 $= 16k$   
 $3k$   
 $= 16k$   
 $3k$   
 $= 16k$   
 $25^{150} = 25^{50} \cdot x^{50}$   
 $25^{150} = x^{50}$   
 $25^{100} = x^{50}$   
 $(5^{2})^{100} = x^{50}$   
 $(5^{2})^{100} = x^{50}$   
 $(5^{2})^{100} = x^{50}$   
 $(5^{2})^{100} = x^{50}$   
 $(5^{4})^{50} = x^{50}$   
 $5^{200} = x^{50}$   
 $(5^{4})^{50} = x^{50}$   
 $(5^{5})^{50} = x^{50}$   
 $(5^{5})^{50}$ 

$$= y^{a^{3}-b^{3}} \cdot y^{b^{3}-c^{3}} \cdot y^{c^{3}-a^{3}}$$

$$= y^{a^{3}-b^{3}+b^{3}-c^{3}+c^{3}-a^{3}}$$

$$= y^{0} = 1$$
[74] (b) Let Salary of Q = 100  
Salary of P = 100 25% of 100  

$$= 100 25$$

$$= 75$$
Salary of R = 100 + 20% of 100  

$$= 100 + 20$$

$$= 120$$
Ratio of salary of R and P = 120 : 75 = 8 : 5  
[75] (b) If x<sup>2</sup> + y<sup>2</sup> = 7xy  
x<sup>2</sup> + y<sup>2</sup> + 2xy = 7xy + 2xy  
(x + y)<sup>2</sup> = 9xy  
taking log on both side  
log (x + y)<sup>2</sup> = log 9xy  
2 log (x + y) = log 9 + log x + log y  
2 log (x + y) = 2 log 3 + log x + log y  
2 log (x + y) = 2 log 3 = log x + log y  
2 log (x + y) = 2 log 3 = log x + log y  
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2 log (x + y) = 2 log 3 = log x + log y  
2 log (x + y) = 2 log 3 = log x + log y  
3 = 2 [log x + log y  
log (x + y) = 1 (log x + log y]  
[76] (b) A person has Assets worth = ₹ 1,48,200  
Ratio of share of wife, son & daughter  
= 3 : 2 : 1  
Sum of Ratio = 3 + 2 + 1 = 6  
Share of Son =  $\frac{2}{6} \times 1,48,200$   
= 49,400  
[77] (c) If x = log<sub>24</sub>12, y = log<sub>36</sub>24 and z = log<sub>48</sub>36 then  
XYZ + 1  
= log<sub>24</sub>12 × log<sub>36</sub>24 × log<sub>48</sub>36 + 1  
=  $\frac{log12}{log24} \cdot \frac{log24}{log36} \cdot \frac{log36}{log48} + 1$ 

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$$= \frac{\log 12}{\log 48} + 1$$

$$= \frac{\log 12 + \log 48}{\log 48}$$

$$= \frac{\log (12 \times 48)}{\log 48}$$

$$= \frac{\log (576)}{\log 48}$$

$$= \frac{\log 24^2}{\log 48}$$

$$= 2 \cdot \frac{\log 24}{\log 48}$$

$$= 2 \cdot \frac{\log 24}{\log 36} \cdot \frac{\log 36}{\log 48}$$

$$= 2 \cdot \log_{36} 24 \cdot \log_{48} 36$$

$$= 2 \cdot y z$$
[78] (a) Given log x = a + b, log y = a b  

$$\log \left(\frac{10x}{y^2}\right) = \log 10x \ \log y^2$$

$$= \log 10 + \log x \ 2\log y$$

$$= 1 + (a + b) \ 2(a \ b)$$

$$= 1 + a + 3b$$
[79] (b) If x = 1 + log\_p qr, y = 1 + log\_q rp, z = 1 + log\_r pq
$$x = \frac{\log p + \log qr}{\log p}$$

$$x = \frac{\log pqr}{\log p}$$

$$x = \frac{\log pqr}{\log p}$$
Similarly
$$\frac{1}{y} = \frac{\log q}{\log pqr}$$

 $\frac{1}{2} = \frac{\log r}{2}$ 

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z logpqr  $\frac{1}{1} + \frac{1}{1} + \frac{1}{2} = \frac{\log p}{1} + \frac{\log q}{1} + \frac{\log q}{1}$ x y z logpqr logpqr logpqr  $= \log p + \log q + \log r$ logpqr \_ logpqr logpqr = 1 [80] (c) Ratio of the salary of a person in three months = 2 : 4 : 5 Salary of  $I^{st}$  month = 2x Let, Salary of  $II^{nd}$  month = 4x Salary of  $III^{rd}$  month = 5x Given (Salary of Product I<sup>st</sup> two months) (Salary of Product of last two months) = 4,80,00,000 (4x.5x) (2x.4x) = 4,80,00,000 $20x^2$   $8x^2 = 4,80,00,000$  $12x^2 = 4,80,00,000$  $x^2 = 40,00,000$ x = 2,000Salary of the person for second month =  $4x = 4 \times 2,000 = 8,000$ [81] (a) Let SP of mixture is ₹ 100 Then Profit = 14.6% of 100 = 14.6 CP of mixture =  $(100 \quad 14.6)$ = 85.4 If SP is ₹ 100 then CP = 85.4 If SP is ₹ 1 then CP = <u>85.4</u> 100 If SP is ₹ 17.60 then CP =  $\frac{85.4}{100}$  × 17.60 = 15.0304 CP of the Mixture per kg = ₹ 15.0304 2<sup>nd</sup> difference = Profit by SP 1 kg of 2<sup>nd</sup> kind @ ₹ 15.0304

$$= 15.54 \quad 15.0304$$
  

$$= 0.5096$$
  
1<sup>st</sup> difference = ₹ 15.0304  $13.84$   

$$= ₹ 1.1904$$
  
The Require Ratio = (2<sup>nd</sup> difference) : (1<sup>st</sup> difference)  

$$= 0.5096 : 1.1904$$
  

$$= 3 : 7$$
  
[82] (d) If  $p^x = q, q^y = r \text{ and } r^z = p^6$   
 $q = p^x, q^y = r \text{ and } r^z = p^6$   
 $[(p^x)^y]^z = p^6$   
 $p^{yz} = p^6 = xyz = 6$   
[83] (a) Log x = m + n and log y = m n  
Then log  $\left(\frac{10x}{y^2}\right)$  = log 10x log y<sup>2</sup>  

$$= \log 10 + \log x \ 2 \log y$$
  

$$= 1 + \log x \ 2 \log y$$
  

$$= 1 + (m + n) \ 2 (m \ n)$$
  

$$= 1 + m + n \ 2m + 2n$$
  

$$= 3n \ m + 1$$
  
[84] (a) If  $15(2p^2 \ q^2) = 7pq$   
 $30p^2 \ 15q^2 = 7pq$   
 $30p^2 \ 15q^2 = 7pq$   
 $30p^2 \ 15q^2 = 7pq$   
 $30p^2 \ 25pq + 18pq \ 15q^2 = 0$   
 $30p^2 \ 25pq + 18pq \ 15q^2 = 0$   
 $30p^2 \ 25pq + 18pq \ 15q^2 = 0$   
 $30p^2 \ 25pq + 3q(6p \ 5q) = 0$   
If  $6p \ 5q = 0$  and  $5p + 3q = 0$   
 $6p = 5q \ 5p = \ 3q$   
 $\frac{p}{q} = \frac{5}{6} = p : q = 5 : 6 \frac{p}{q} = \frac{-3}{5}$   
(not possible)  
[85] (b) The third proportion of 12,30  
 $c = \frac{b^2}{a} = \frac{(30)^2}{12} = \frac{900}{12} = 75$   
The Mean proportion of 9,25  
 $b = \sqrt{ac} = \sqrt{9 \times 25} = \sqrt{225} = 15$ 

Ratio of third proportion of 12, 30 and Mean proportion of 9, 25 = 75:15 = 5:1 **[86] (c)**  $\log_5 3 \times \log_3 4 \times \log_2 5$  $= \frac{\log 3}{\log 5} \times \frac{\log 4}{\log 3} \times \frac{\log 5}{\log 2}$  $= \frac{\log 4}{\log 2}$  $= \frac{\log 2^2}{\log 2}$  $=\frac{2\log 2}{\log 2}=2$ [87] (a) Let x to be added Then (10 + x), (18 + x), (22 + x), (38 + x) are in prop. Product of Extremes = Product of Mean (10 + x) (38 + x) = (18 + x) (22 + x) $380 + 10x + 38x + y^2 = 396 + 18x + 22x + y^2$ 48x + 380 = 396 + 40x48x - 40x = 396 - 3808x = 16 x = 2 [88] (b)  $\frac{2^{n}+2^{n-1}}{2^{n+1}-2^{n}} = \frac{2^{n}+2^{n}.2^{-1}}{2^{n}.2^{1}-2^{n}}$  $= \frac{2^{p}(1+2^{-1})}{2^{p}(2^{1}-1)}$  $= \frac{\left(\frac{1}{1}+\frac{1}{2}\right)}{(2-1)}$  $\left(\frac{2+1}{2}\right)$ 

$$=\frac{\left(\frac{2+1}{2}\right)}{1}$$
$$=\left(\frac{3}{2}\right)$$

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[89] (b)	The integral part of a logarithms is called <b>Characteristic</b> and the decimal part of a logarithm is called <b>mantissa</b> .			
[90] (b)	$\frac{x^2 - (y - z)^2}{(x + z)^2 - y^2} + \frac{y^2 - (x - z)^2}{(x + y)^2 - z^2} + \frac{z^2 - (x - y)^2}{(y + z)^2 - x^2}$			
	$=\frac{(x+y-z)(x-y+z)}{(x+z+y)(x+z-y)} + \frac{(y+x-z)(y-x+z)}{(x+y+z)(x+y-z)} + \frac{(z+x-y)(z-x+y)}{(y+z+x)(y+z-x)}$			
	$=\frac{x+y-z}{x+y+z}+\frac{y+z-x}{x+y+z}+\frac{z+x-y}{x+y+z}$			
	$= \frac{x + y - z + y + z - x + z + x - y}{x + y + z}$			
	$=\frac{x+y+z}{x+y+z}=1$			
[91] (d)	Given x = 3y and y = $\frac{2}{3}z$			
	$\frac{x}{y} = \frac{3}{1}$ and $\frac{y}{z} = \frac{2}{3}$			
	x : y = 3 : 1 and y : z = 2 : 3 = 3 × 2 : 1 × 2			
	= 3 × 2 : 1 × 2 = 6 : 2			
<b>1001</b> ( )	x: y: z = 6: 2: 3			
[92] (c)	If $\log_4 (x^2 + x) - \log_4 (x + 1) = 2$ ( (x <sup>2</sup> +x))			
	$\log_4\left\{\frac{(x^2+x)}{(x+1)}\right\}=2$			
	$\log_4 \left\{ \frac{\mathbf{x}(\mathbf{x}+1)}{(\mathbf{x}+1)} \right\} = 2$			
	$\log_4 x = 2$ x = 4 <sup>2</sup>			
[02] /L)	x = 16 1 . 1 . 1			
[93] (b)	$\frac{1}{\log_3 60} + \frac{1}{\log_4 60} + \frac{1}{\log_5 60}$			
	$- \log 2 \log 4 \log 5$ $\begin{bmatrix} 1 \\ -\log 2 \end{bmatrix}$			
	$= \log_{60} 3 + \log_{60} 4 + \log_{60} 5 \qquad \left[ \Box \frac{1}{\log_{a} b} = \log_{b} a \right]$			
	$= \log_{60}(3 \times 4 \times 5)$			

$$= \log_{e0} 60$$

$$= 1$$
[94] (c) If  $3^{x} = 5^{y} = 75^{z} = k (let)$ 
then  $3^{x} = k$ ,  $5^{y} = k$ ,  $75^{z} = k$   
 $3 = k^{1/x}$ ,  $5 = k^{1/y}$ ,  $75 = k^{1/z}$ 
we know that
$$75 = 3 \times 5 \times 5$$
 $\frac{1}{k^{\frac{1}{2}}} = \frac{1}{k^{\frac{1}{x}}}, \frac{1}{k^{\frac{1}{y}}}, \frac{1}{k^{\frac{1}{y}}}$ 
 $\frac{1}{k^{\frac{1}{z}}} = \frac{1}{k^{\frac{1}{x}}}, \frac{1}{y}, \frac{1}{y}$ 
on comparing
$$\frac{1}{k^{\frac{1}{z}}} = \frac{1}{k^{\frac{1}{x}}}, \frac{1}{y}, \frac{1}{y}$$

$$\frac{1}{k^{\frac{1}{z}}} = \frac{1}{k^{\frac{1}{x}}}, \frac{1}{y}, \frac{1}{y}$$
[95] (c) If log 2 = 0.3010 and log 3 = 0.4771
then log 24 = log (2 \times 2 \times 2 \times 3)
 $= log 2 + log 3$ 
 $= 3 \log 2 + log 3$ 
 $= 3 \log 2 + log 3$ 
 $= 3 (0 3010 + 0.4771)$ 
 $= 0.9030 + 0.4771$ 
 $= 1.3801$ 
[96] (a) If  $abc = 2$ 
 $ab = \frac{2}{c} = 2c^{-1}$ 
 $a = \frac{2}{bc} = 2b^{-1}c^{-1}$ 
 $bc = \frac{2}{a} = 2a^{-1}$ 
 $b = \frac{2}{ca} = 2c^{-1}a^{-1}$ 
 $ca = \frac{2}{b} = 2b^{-1}$ 
 $c = \frac{2}{ab} = 2b^{-1}$ 
Given  $\frac{1}{1+a+2b^{-1}} + \frac{1}{1+\frac{1}{2}b+c^{-1}} + \frac{1}{1+c+a^{-1}}$ 

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## CPT Solved Scanner : Quantitative Aptitude (Paper 4)

 $= \frac{1}{1+a+2b^{-1}} + \frac{2b^{-1}}{2b^{-1}(1+\frac{1}{2}b+c^{-1})} + \frac{a}{a(1+c+a^{-1})}$   $= \frac{1}{(1+a+2b^{-1})} + \frac{2b^{-1}}{2b^{-1}+1+2b^{-1}c^{-1}} + \frac{a}{a+ac+1}$   $= \frac{1}{1+a+2b^{-1}} + \frac{2b^{-1}}{2b^{-1}+1+a} + \frac{a}{a+2b^{-1}+1}$   $= \frac{1+2b^{-1}+a}{1+a+2b^{-1}}$  = 1

[97] (a)	let	Total no. of coins Ratio of ₹ 1 coin : ₹ 2 coins No. of ₹ 1 coins No. of ₹ 2 coins No. of ₹ 5 coins	= 23 = 3 : 2 = 3x = 2x = 23-3x-2x = 23-5x			
	Total value of all coins = 43					
	3x >	$(1 + 2x \times 2 + (23 - 5x))5 = 43$				
	3x -	+ 4x + 115 – 25x = 43				
		– 18x = 43 – 115				
		– 18x = – 72				
		$x = \frac{-72}{-18} = 4$				
	No.	of ₹ 1 coins = 3x = 3 × 4 = 12				